

Evaluating the Effectiveness of Storage Control in Reducing Peak Demand on Low Voltage Feeders

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ABSTRACT

Uptake of Low Carbon Technologies is likely to lead to increased demand in distribution networks and consequently could impose additional stress on the networks. Battery Energy Storage Systems (BESS) are identified as a feasible alternative to traditional network reinforcement. This paper analyses two BESS scheduling algorithms (Model Predictive Control (MPC) and fixed schedule) supplied with forecasts from five methods for predicting demand on 100 low voltage feeders. Results show that forecasting feeders with higher mean daily demand produces lower mean absolute errors and better peak demand reduction. MPC with simple error improves peak reduction over fixed schedule for feeders with lower mean daily demand.

INTRODUCTION

In the transition towards the Low Carbon Economy, increased electricity demand is expected through the uptake of low carbon technologies (LCTs). Operation of heat pumps and uncontrolled charging of electric vehicles will impose additional stress on the electricity distribution networks [1]. In the UK, the additional demand from LCTs typically coincides with the usual evening peak demand and, therefore, potentially violates the thermal operational constraints on the networks. Traditionally when the thermal capacity of the network has reached the limit, distribution networks are reinforced by replacing the existing assets (e.g. transformers and feeder cables) with higher rating or installing additional assets to split the load. However, as well as being expensive, such reinforcements are inefficient since the thermal constraints are occurring over relatively short periods of time and the remaining time these assets remain underutilised.

With the decreasing costs of electro-chemical energy storage, deployment of Battery Energy Storage Systems (BESS) becomes an effective alternative solution for the deferral of traditional reinforcement of the distribution networks [2-5]. The control strategy applied to BESS, and its size, depends on the location and the purpose of its operation, i.e. peak demand reduction, peak generation reduction and voltage support [6]. One of the most popular and versatile control methods is Model Predictive

Control (MPC) which uses a forecast as prior knowledge to plan an optimal BESS charging and discharging schedule whilst adjusting the schedule based on observed demand [7-9].

Due to individuality of customer behaviour and the number of customers on Low Voltage (LV) feeders, predicting the demand is much more difficult than on higher voltage levels of the distribution network.

This paper presents an analysis of a scheduling MPC algorithm with a fixed error correction method versus a fixed schedule, applied to a simulated BESS, to reduce peak demand on Low Voltage (LV) feeders based on five forecasting methods. The forecasts, the MPC algorithm and the fixed schedule are assessed on two weeks of half-hourly demand data from 100 LV feeders monitored as part of the New Thames Valley Vision [10] – an LCNF project, funded by Ofgem and led by Scottish and Southern Electricity Networks. The feature of this paper is application of the fixed schedule and MPC algorithm for a BESS on demand data from 100 real LV feeders using four advanced forecasting techniques.

METHOD

Performance of the control algorithm applied to the BESS is an important factor. Forecast error and poor algorithm performance could result in scheduling BESS to charge at the same time as the actual peak. Higher peak would then lead to further violation of the operational constraints and potentially, equipment failure.

To investigate the relationship between the achieved peak demand reduction and the forecast method, two control algorithms are considered: fixed optimal schedule and MPC with fixed error demand model update. The algorithms are applied to a simulated BESS on a LV distribution feeder in a suburban network. The BESS is sized to deal with 20% reduction of the forecasted demand aggregated across the 3 phases.

Schedule optimisation

The aim of the schedule optimisation is to find a BESS schedule, \mathbf{p} , for the forecasted demand, \mathbf{d}_f over a period of N half-hours (in this case 48), such that the cost function in (1) is minimised:

$$F(\mathbf{p}, \mathbf{d}_f) = \xi_p(\mathbf{p}, \mathbf{d}_f) + \frac{\alpha \xi_{cd}(\mathbf{p})}{w} + \frac{\beta \xi_{sc}(\mathbf{c})}{w} + \frac{\gamma \xi_{ts}(\mathbf{c})}{w}, \quad (1)$$

Subject to constraints:

$$C_{\min} \leq c(t) \leq C_{\max}, \quad (2)$$

$$P_{\min} \leq p(t) \leq P_{\max}, \quad (3)$$

$$c(t+1) = c(t) + p(t)\mu\tau, \quad (4)$$

$$\mu = \begin{cases} \mu & \text{if } p(t) \geq 0 \\ \frac{1}{\mu} & \text{if } p(t) < 0 \end{cases} \quad (5)$$

$$\alpha, \beta, \gamma \in [0,1]. \quad (6)$$

Where, $\xi_p(\mathbf{p}, \mathbf{d}_f)$ is the Peak-to-Average cost component for peak reduction, self-normalised to the initial conditions, defined as:

$$\xi_p(\mathbf{p}, \mathbf{d}_f) = \frac{\left(\frac{\max_{t=1, \dots, N} (d(t)+p(t))}{\sum_{t=1}^N (d(t)+p(t))/N} \right)^2}{\xi_p(\mathbf{p}_i, \mathbf{d}_f)}. \quad (7)$$

Cost component, ξ_{cd} , represents the cost of charge dynamics, aimed at smoothing the charging of BESS and defined as:

$$\xi_{cd} = \frac{\max\left(\left|\frac{\delta I_{[0, p_{\max}]}(p)}{\delta t}\right|\right)}{p_{\max}}. \quad (8)$$

The storage cycling cost component, ξ_{sc} , aims to allow at most only one full charge and discharge cycle per day and defined as:

$$\xi_{sc} = \frac{\sum_{t=1}^N \left| \frac{\delta I_{[0, p_{\max}]}(c)}{\delta t} \right| + \sum_{t=1}^N \left| \frac{\delta I_{[-p_{\max}, 0]}(c)}{\delta t} \right|}{2}. \quad (9)$$

At the end of the schedule, the BESS should reach 50% State-of-Charge (SoC), which is achieved with the target SoC cost component, ξ_{ts} , defined as:

$$\xi_{ts}(c) = \frac{(c(N) - 0.5C_{\max})^2}{\xi_{ts}(c_i)}. \quad (10)$$

Scaling factor, w , ensures that sum of cost components ξ_{cd} , ξ_{sc} and ξ_{ts} is at the same scale as ξ_p :

$$w = \alpha + \beta + \gamma \quad (11)$$

Constraints in (2) and (3), represent limits on the energy storage capacity, $c(t)$, and BESS power rating constraints, respectively. A model for the energy storage is given in (4) where τ is the duration of the time period in hours and μ is the BESS efficiency defined in (5).

Model predictive control for BESS

MPC, also known as receding horizon control, computes an optimal schedule for the duration of the horizon by updating the demand model with recent observations and deploying only the first control value from the current horizon. Once the control for the first time step is deployed and observation for the current time step is received, the controller moves to the next horizon to compute a new optimal schedule on the updated demand model.

In this case study, MPC doesn't have access to the demand model used in generating the forecasts and so is not able to produce rolling forecasts. Instead the demand is modelled by updating the forecast with the projection of the forecast error from the previous time step, as depicted in Figure 1 and it is assumed that all forecast errors are strongly positively correlated. This clearly will not be the case in general.

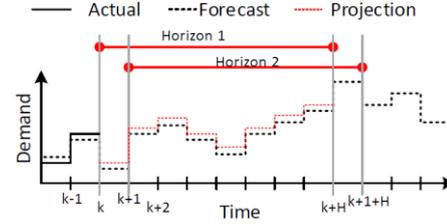


Figure 1: MPC horizons and error projection within the horizon.

The length of the horizon is chosen to be 10 half-hourly time steps [9]. The controller is optimising the same cost function as for the fixed schedule in eq. (1), reduced to the length of the control horizon.

The input demand profile, \mathbf{d}_f , is replaced for the duration of the horizon H_k with the forecast, \mathbf{d}_f^* , shifted by error, $e(k+1)$. The error is based on the observed demand at the previous time step (excluding the energy exchanged with BESS) and the original forecast at the previous times step, (as depicted in Figure 2.).

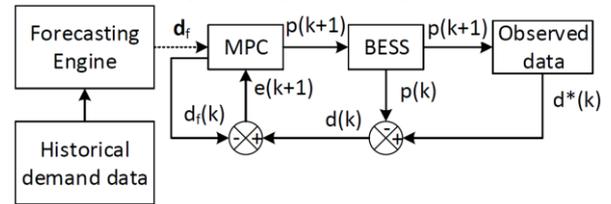


Figure 2: Data flow diagram for MPC in this paper.

Peak reduction metrics

The case study consists of three scenarios:

- “Best possible” – Fixed schedule based on the assuming 100% accurate forecast
- “Fixed” – fixed schedule based on forecast
- “MPC” – receding horizon control with fixed error

For each scenario the peak reduction metric is given as:

$$PR(\mathbf{d}^*) = \left(1 - \frac{\max(\mathbf{d}^*)}{\max(\mathbf{d}_o)}\right) \times 100\%,$$

where \mathbf{d}^* denotes the resultant demand on the feeder by applying the corresponding schedule and \mathbf{d}_o is the observed demand profile. This metric considers only the overall peak reduction on demand over the entire day, not just the reduction of the observed peak.

Demand data

The demand data used in this case study is based on the monitoring of the LV substations in Bracknell, Berkshire, UK as part of the New Thames Valley Vision project [10]. The data set is based on energy consumption recorded on 100 LV feeders between the 31st of March 2014 and 14th of November 2015. The first 83 weeks were used for training the forecast methods and the last two weeks were used for testing.

Forecasting methods

We consider 5 basic load forecast to apply in our control method, summarised below:

1. **7SAV** is our benchmark method and forecasts each time period, e.g. 10 a.m. on Thursday is simply the average of the previous 5 10 a.m.'s on Thursday.
2. **ST** is a simple seasonal model for each hour. It is the same as that as presented in [11] but there is now a dummy variables for each day type (Monday, Tuesday etc.)
3. **Snt** is as **ST** but no annual linear trend is modelled.
4. **GAM**, which stands for Generalised Additive Model, is a simple generalised model based on that in [12, 13] which estimates the electricity load using a piecewise smooth function determined from the predictor variable(s). Here we consider only one predictor variable to forecast the electricity load, that is, the electricity load from the half hour two days prior. Note that we do not include weather variables.
5. **ARWD** is a simple autoregressive method which is typically used for electricity price forecasting [14]. It is based on a two-step approach. In the first one, the weekly load profile μ_t is estimated for every hour of the week. A residual time series r_t is then created by subtracting the time series from the historical load $r_t = L_t - \mu_t$, where L_t is the load at time t . In the second step an AR(p) process (autoregressive process of order p) which satisfies

$$r_t = \varphi_0 + \sum_{k=1}^p \varphi_k r_{t-k} + \varepsilon_t$$
 with parameters φ_k and error term ε_t is estimated by solving the Yule-Walker equations. The p is chosen so that the Akaike Information Criterion (AIC) is minimised with a maximal possible value of $p_{max} = 48 \times 15$.

RESULTS

Forecast

On average over all 100 feeders the best performing methods were the **ARWD** method and the simple average **7SAV** with MAPEs of 17.72 and 18.60 respectively, the seasonal methods **Snt** and **ST** also performed well with average MAPEs of 18.76 for the **ST** method and 19.05 for the **Snt** method. The worst performing method was the **GAM** with a MAPE of 27.54. We note that the **ST** and **Snt** methods have very similar performances. It was also found that certain methods performed better than others for different feeders. For instance the best scoring method for 48 of the feeders was the **ARWD** method, followed by **Snt** and **ST** with 14 and 31 respectively. Finally the **7SAV** method was best for the remaining 7 feeders. This indicates that different forecasts methods should perhaps be used for different feeders. Identification of why this is the case will be future work.

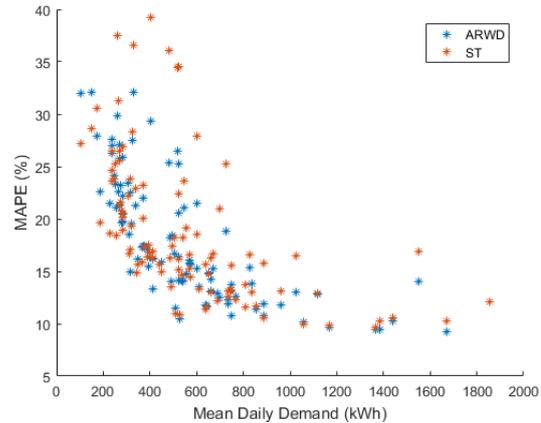


Figure 3: Relationship between MAPE and Mean daily energy demand for each feeder for two of the forecast methods.

The relationship between mean daily demand (for the last year) and the errors are shown in Figure 3 for **ARWD** and **ST**. It clearly shows the methods have smaller relative errors for the larger substations as expected.

From these results we therefore expect the best methods to be the **ARWD**, the **ST** and the **Snt**. We'd also expect bigger peak reductions for larger feeders since the demands are more predictable and therefore the control can be more effective.

Peak reduction

Figure 4 shows the boxplot for peak reduction for each control method, each forecast method and the best possible peak reduction, $PR(d_a^*)$. Overall, on average all forecast methods and control techniques achieved some peak reduction. The least increase on the peaks was achieved by **ARWD**. Yet, on average **Snt** provided best peak reduction for both fixed and MPC, closely followed by **ARWD**. Figure 5 shows **Snt** forecast against observed demand and resultant demand with BESS schedules.

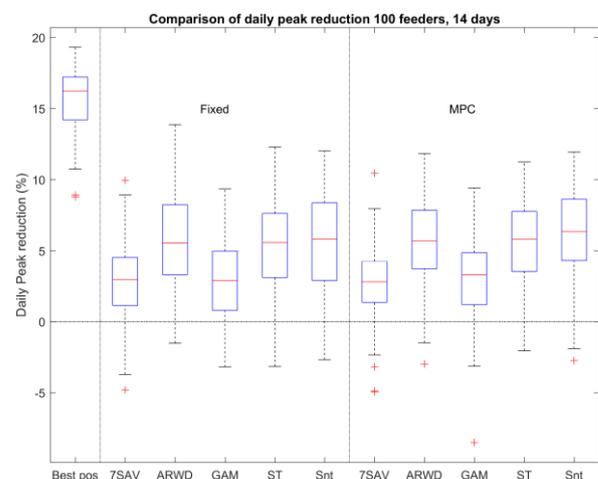


Figure 4: Comparison of the daily peak reduction for each forecasting method and each scenario: $PR(d_o^*)$, $PR(d_f^*)$ and $PR(d_m^*)$.

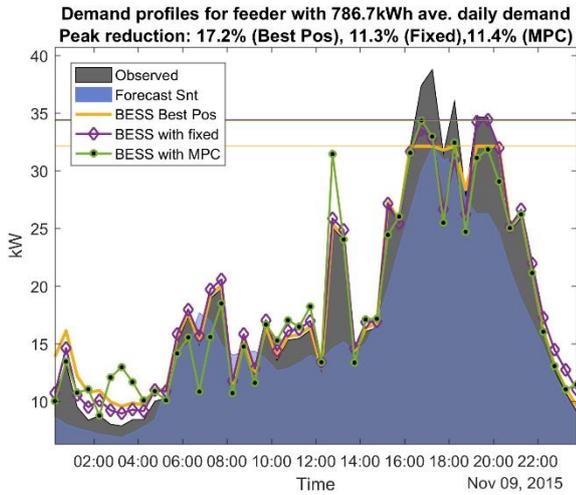


Figure 5: Observed, forecasted demand and profiles resulting from best possible, fixed and MPC schedules based on **Snt** forecasting method.

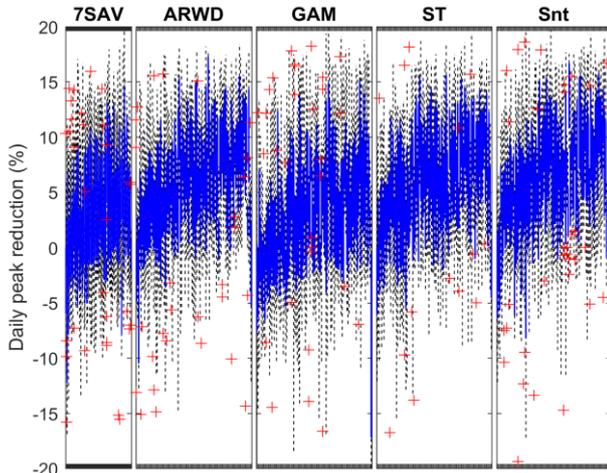


Figure 6: Daily peak reduction against ascending mean demand per feeder for each forecasting method based on “MPC” scenario.

Comparison of Figure 6 and the overall mean peak reduction in table 1 shows that there is no clear performance improvement of MPC with simple error over the fixed schedule averaged for all feeders. Day-wise and feeder-wise comparison in Table 2 shows that MPC with fixed error performs better than fixed schedule about half-of the time.

Table 1: Overall mean peak reduction, $PR(d_f^*)$ and $PR(d_m^*)$, for Fixed and MPC algorithms respectively over all feeders and days for each forecasting method.

	7SAV	ARWD	GAM	ST	Snt
Fixed	2.85%	5.63%	2.87%	5.53%	5.57%
MPC	2.77%	5.68%	3.00%	5.57%	6.17%

Table 2: Percentage of all days on all 100 feeders when MPC achieved better peak reduction than fixed schedule

7SAV	ARWD	GAM	ST	Snt
46.6%	50.1%	50.2%	49.1%	52.5%

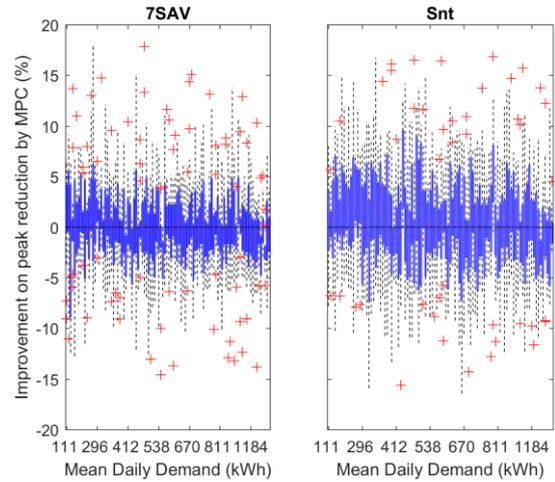


Figure 7: Percentage of days when MPC performed better than fixed schedule in daily peak reduction for the worst and the best forecasts, **7SAV** and **Snt** respectively.

The results here confirm firstly that the more accurate forecasting methods produce the greatest peak reduction. Secondly we can also see there is a clear relationship between peak reduction and the mean daily demand of the feeder. As expected, due to the volatility of small feeders, in these cases the control methodologies on average actually increases the size of the peak. Figure 7 suggests a potential relationship between improved peak reduction with MPC and mean daily demand, with smaller feeders to have better peak reduction than the fixed schedule.

DISCUSSION

Comparison of MAPE for a range of feeder sizes shows that some forecast perform better for certain types of feeders. Hence there was no one forecast that suited all feeders. We tested a number of forecast methods against a competitive benchmark. An advantage of all methods is their simplicity and computational speed in being implemented.

Forecast accuracy is a strong driver for potential peak reduction but accuracy was driven strongly by mean daily demand on the feeder. Hence the effectiveness of storage is linked to the number of customers on a feeder and the size of these customers. As the result, better peak reduction was achieved with fixed schedule and MPC with simple error correction for the feeders with greater mean daily demand. For small feeders BESS with fixed schedule actually increases the peak demands. Hence there should be a minimum size threshold when deciding if a feeder is suitable for BESS with scheduling algorithms. However, MPC with the fixed error demand update method, performed better than fixed schedule, particularly on smaller feeders. Further investigation is required on the correlation of forecast errors and demand characteristics on smaller feeders. More sophisticated error modelling techniques (e.g. rolling forecast) are

expected to improve the performance of MPC, especially on larger feeders.

In case of operational implementation of BESS on a LV distribution feeder, the control system is typically based on multiple stages: planning and real-time operation. The real-time operation control is happening at a much higher resolution than the half-hourly planning stage. The half-hourly demand represents an average power within the half-hour meaning that the actual peaks measured at the higher-resolution (e.g. 5 seconds or one minute) would be significantly greater than the half-hourly average.

Furthermore, this paper only considered aggregated demand across 3 phases at half-hourly resolution. Due to the number of customers on each phase and their individual behaviour, the demand is likely to be unbalanced. Although balancing the demand on the phases would not decrease the aggregated half-hourly demand, peaks on each phase measured at higher resolution are likely to be significantly reduced, assisting with managing the thermal constraints on the feeder.

SUMMARY

The paper has presented a comparison of five forecasting techniques for prediction of LV feeders and their role in the reduction of peak demand using two energy storage control techniques: fixed schedule and model predictive control. The forecasting techniques and control algorithms have been assessed on demand data for 14 days from 100 LV feeders.

Results show that certain type of forecasts perform better for certain sizes of feeders and consequently lead to better performance of the peak reduction algorithms. Both fixed schedule and MPC with simple error achieved better peak reduction for larger feeders. However, MPC with simple error correction have performed better on smaller feeders compared to the fixed schedule.

In future work, integration of advanced demand models and rolling forecast for the model predictive control will be considered.

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